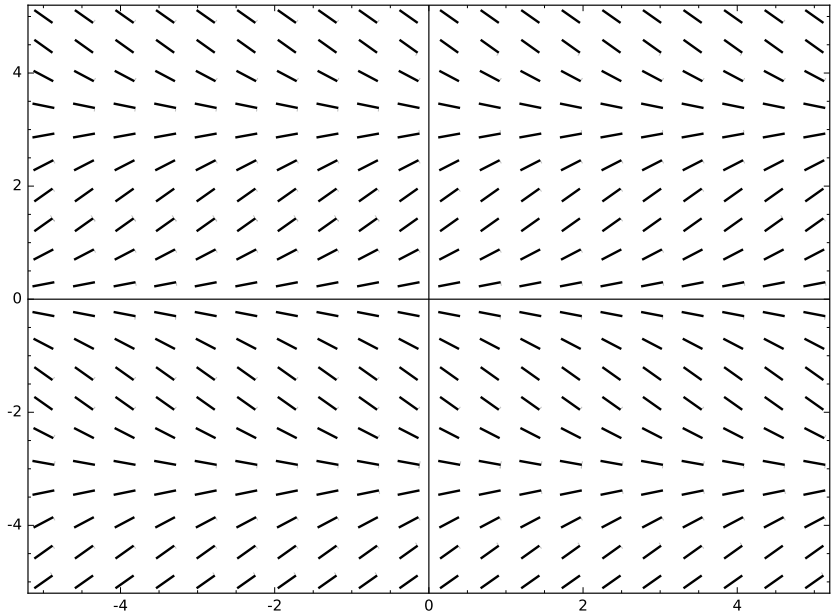
1. Which of the following is a true statement about the critical points of the autonomous ODE $y' = y^2 - 2y + 1$?

(A) It has more than one critical point.

(B) It has exactly one critical point, and it is unstable.

(C) It has exactly one critical point, and it is stable.

2. Which of the following first order ODEs could the depicted slope field belong to?



(A) $y' = \sin(y)$

(B) $y' = y^2$

(C) $y' = x + y$

(D) None of the above

3. The first order ODE $x' = \sin(t)x$ is...

(A) Separable and linear.

(B) Separable but not linear.

(C) Linear but not separable.

(D) Neither separable not linear.

4. True or False?

The initial value problem

$$y' = xy^2 - y, \quad y(0) = 2$$

has a unique solution.

5. Suppose y is a function such that $y' = y^2 - 1$ and $y(0) < 1$. What is $\lim_{x \to \infty} y(x)$?

(A) -1

(B) 0

(C) 1

(D) None of the above

6. True or False?

The initial value problem

$$(y - x^2)y' = 0, \quad y(0) = 0$$

has a unique solution.

7. Suppse you're solving the nonhomogeneous second order ODE

$$x'' + 4x = \cos(2t)$$

using the method of undetermined coefficients. What form should you guess for the particular solution?

(A) $x_p = a\cos(2t)$

(B) $x_p = a\cos(2t) + b\sin(2t)$

(C) $x_p = at\cos(2t) + bt\sin(2t)$

(D) None of the above

8. How might you go about solving the first order ODE $y' + 3y = e^x$?

(A) Separating variables.

(B) Integrating factors.

(C) Neither of the above.

9. If you're solving the ODE $y' + 3y = e^x$ using integrating factors, what is the integrating factor?

(A) e^{3x}

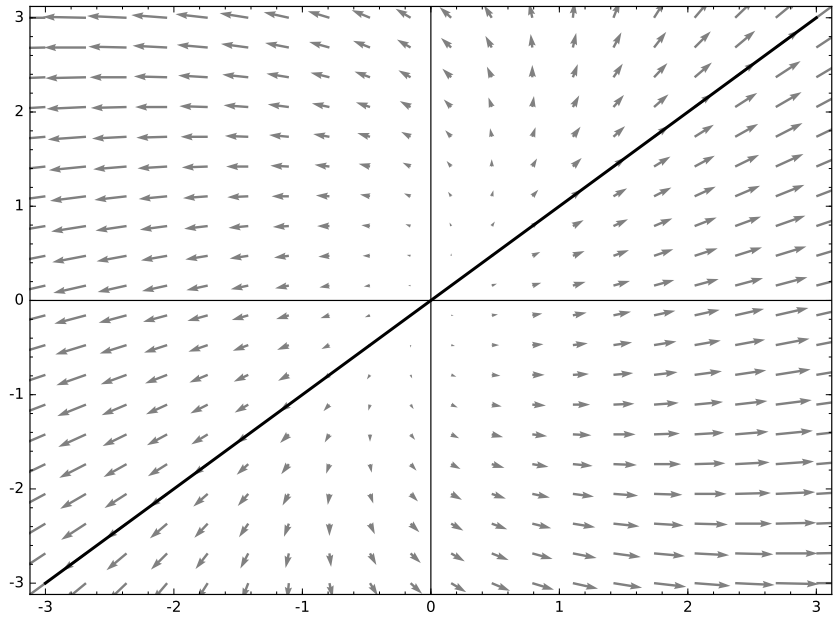
(B) e^{-3x}

(C) e^3

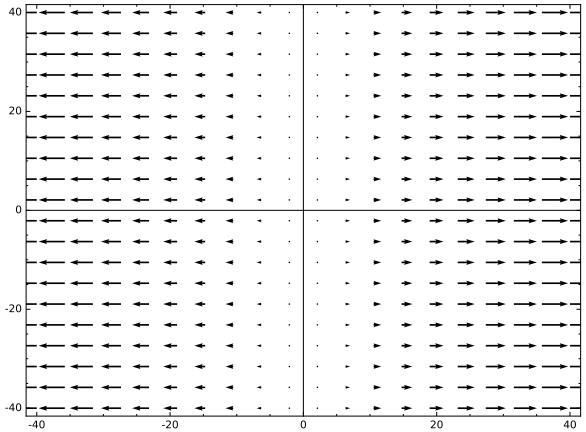
(D) None of the above

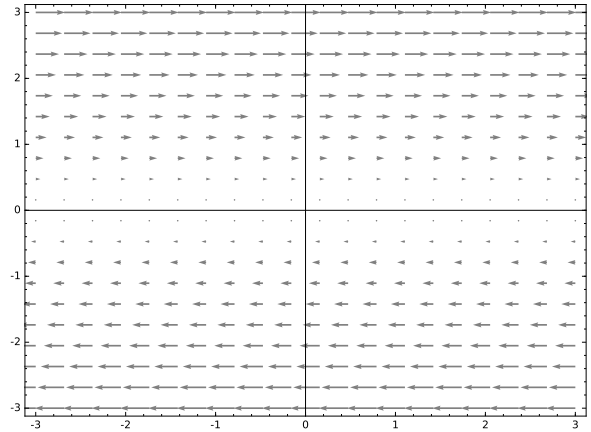
10. True or False?

If the depicted phase portrait belongs to a system $\vec{x}' = A\vec{x}$ for a 2×2 matrix A, then A must have a positive deficient eigenvalue.



11. Consider the following two phase portraits, which belong to the linear systems $\vec{x}' = A\vec{x}$ and $\vec{x}' = B\vec{x}$, respectively.





Which of the following is true?

(A) A has $\lambda = 0$ as a complete eigenvalue.

(B) B has $\lambda = 0$ as a deficient eigenvalue.

(C) Both the above.

(D) None of the above.

12. True or False?

If X is any fundamental matrix solution for a linear homogeneous system $\vec{x}' = A\vec{x}$, then

$$X' = AX.$$

13. True or False?

If X is any fundamental matrix solution for a linear homogeneous system $\vec{x}' = A\vec{x}$, then

$$X' = XA.$$

Follow-up. What about $X = e^{At}$?